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## TURBINE APPARATUS AND GOVERNOR FOR TURBINE

## BACKGROUND OF THE INVENTION

The present invention relates to a turbine apparatus especially of low specific speed including a turbine runner and a governor for controlling a rotational speed of the turbine runner.

Generally in a turbine apparatus of low specific speed, so-called S characteristics as shown in Figs. 1A and 1B occur, and the turbine apparatus is controlled as disclosed by JP-A-2002-303244 to be restrained from being made unstable in its operation by the S characteristics.

## BRIEF SUMMARY OF THE INVENTION

An object of the present invention is to provide a turbine apparatus of low specific speed and a governor for controlling a rotational speed of a turbine runner, by which the turbine runner can be rotated stably irrespective of S characteristics even when a head of a water for driving the turbine runner is low.

In a turbine apparatus to be driven by a water, comprising a runner rotatable to be rotationally driven by the water, a flow rate adjuster for adjusting a flow rate of the water to change an actual rotational speed of the runner, and a control device for

generating a control signal for controlling the flow rate adjuster so that a difference between the actual rotational speed of the runner and a desired rotational speed of the runner is decreased, wherein the control

5 device includes an input port for receiving a runner speed signal whose value corresponds to the actual rotational speed of the runner so that an input signal whose value corresponds to the difference between the actual rotational speed of the runner and the desired

10 rotational speed of the runner is generated, a derivative calculation element for generating a derivative component of the control signal whose value corresponds to a value to be applied to the derivative calculation element and the integration calculation

15 element by performing differentiation on the value of the input signal with respect to a time proceeding and an integration calculation element for generating an integral component of the control signal whose value corresponds to a value to be applied to the derivative

20 calculation element and the integration calculation element by performing integration on the value of the input signal with respect to the time proceeding, and

a ratio of a gain of the derivative calculation element to a gain of the integration

25 calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired

rotational speed of the runner is not more than a predetermined degree is greater than a ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree.

10            Since the ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than a predetermined degree is greater than a ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree, even when the head of the water for driving the turbine runner is low and the actual rotational speed of the runner increases to the vicinity of the desired rotational speed of the runner so that an operating point of the runner is positioned

in a so-called S-characteristic portion as defined  
below in the present application, the derivative  
component of the control signal effectively suppresses  
an undesirable oscillation in the rotational speed of  
5 the runner.

It is preferable for keeping an acceleration  
in the rotational speed of the runner from zero toward  
the desired rotational speed thereof not too slow that  
the ratio of the gain of the derivative calculation  
10 element to the gain of the integration calculation  
element to be applied to the derivative calculation  
element and the integration calculation element when  
the difference between the actual rotational speed of  
the runner and the desired rotational speed of the  
15 runner is not more than the predetermined degree is  
greater than a ratio of the gain of the derivative  
calculation element to the gain of the integration  
calculation element to be applied to the derivative  
calculation element and the integration calculation  
20 element when the difference between the actual  
rotational speed of the runner and the desired  
rotational speed of the runner is more than the  
predetermined degree when the head of the water for  
driving rotationally the runner is not more than a  
25 predetermined value, and the ratio of the gain of the  
derivative calculation element to the gain of the  
integration calculation element to be applied to the  
derivative calculation element and the integration

calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree is prevented from being greater than the ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree, when the head of the water for driving rotationally the runner is more than the predetermined value.

It is preferable for keeping the acceleration in the rotational speed of the runner from zero toward the desired rotational speed thereof not too slow at least when  $Q$  is the flow rate of the water for driving rotationally the runner,  $H$  is the head of the water for driving rotationally the runner,  $N$  is the actual rotational speed of the runner,  $T$  is a torque for driving rotationally the runner,  $N_1 = N/\sqrt{H}$ ,  $Q_1 = Q/\sqrt{H}$ ,  $T_1 = T/H$ ,  $\partial Q_1/\partial N_1 \leq 0$ ,  $\partial T_1/\partial N_1 \leq 0$ , the absolute value of  $\partial Q_1/\partial N_1$  is not more than a first value, and the absolute value of  $\partial T_1/\partial N_1$  is not more than a second value, that is, the operating point of the runner is not in the S-characteristic portion or in the vicinity of the S-characteristic portion that the ratio of the gain of

the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree is greater than the ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree, under at least one of a case in which  $\partial Q_1/\partial N_1 > 0$ , a case in which  $\partial T_1/\partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1/\partial N_1$  is more than the first value, and a case in which an absolute value of  $\partial T_1/\partial N_1$  is more than the second value (that is, an operating point of the runner is in the so-called S-characteristic portion or in the vicinity of the S-characteristic portion), and the ratio of the gain of the derivative calculation element to the gain of the integration calculation element be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than a predetermined degree is prevented from being greater

than the ratio of the gain of the derivative  
calculation element to the gain of the integration  
calculation element to be applied to the derivative  
calculation element and the integration calculation  
5 element when the difference between the actual  
rotational speed of the runner and the desired  
rotational speed of the runner is more than the  
predetermined degree, under a case in which  $\partial Q_1/\partial N_1 \leq 0$ ,  
 $\partial T_1/\partial N_1 \leq 0$ , the absolute value of  $\partial Q_1/\partial N_1$  is not more than  
10 the first value, and the absolute value of  $\partial T_1/\partial N_1$  is  
not more than the second value.

It is preferable for keeping the acceleration  
in the rotational speed of the runner from zero toward  
the desired rotational speed thereof not too slow at  
15 least when the difference between the actual rotational  
speed of the runner and the desired rotational speed of  
the runner is more than the predetermined degree, that  
during an increase of the actual rotational speed of  
the runner from zero toward the desired rotational  
20 speed of the runner, the ratio of the gain of the  
derivative calculation element to the gain of the  
integration calculation element applied to the  
derivative calculation element and the integration  
calculation after the difference between the actual  
25 rotational speed of the runner and the desired  
rotational speed of the runner becomes not more than  
the predetermined degree is greater than the ratio of  
the gain of the derivative calculation element to the

gain of the integration calculation element applied to the derivative calculation element and the integration calculation before the difference between the actual rotational speed of the runner and the desired rotational speed of the runner becomes not more than the predetermined degree.

The gain of the derivative calculation element applied to the derivative calculation element and the integration calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree may be not less than the gain of the derivative calculation element applied to the derivative calculation element and the integration calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree, and the gain of the integration calculation element applied to the derivative calculation element and the integration calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree may be less than the gain of the integration calculation element applied to the derivative calculation element and the integration calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than



the predetermined degree.

It is preferable for controlling the actual rotational speed of the runner stably at least when an electric power generator driven by the runner is being

5   synchronized to be electrically connected to electric power transmission lines that a first ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration

10   calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree is greater than a second ratio of the gain of the derivative calculation element to the

15   gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the

20   predetermined degree, when the electric power generator is prevented from supplying the electric power to the electric power transmission lines or before the electric power generator driven by the runner is electrically connected to the electric power

25   transmission lines, and a third ratio of the gain of the derivative calculation element to the gain of the integration calculation element to be applied to the derivative calculation element and the integration

calculation when the electric power generator is electrically connected to the electric power transmission lines is smaller than the first ratio of the gain of the derivative calculation element to the gain of the integration calculation element.

The runner may be rotatable in either of a normal direction for being driven by the water and a reverse direction for pumping the water when the runner is prevented from being operated to drive the electric power generator.

When the turbine apparatus further comprises a proportional calculation element for generating a proportional component of the control signal whose value is proportional to the value of input signal, and the control device is a governor in accordance with the IEC International Standard 61362 First Edition, it is preferable that the gain of the derivative calculation element is more than 5 and a gain of the proportional calculation element is less than 0.5, when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree. In this case, it is more preferable that the gain of the proportional calculation element is more than 0.6, when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is more than the predetermined degree.

It is preferable that the flow rate of the

water for driving the runner is rapidly increased just after or in response to that the electric power generator driven by the runner is electrically connected to electric power transmission lines to supply the electric power from the electric power generator to the electric power transmission lines after the actual rotational speed of the runner is synchronized in S-characteristic portion of the runner with required frequency of alternating electric current of the electric power transmission lines, from the flow rate of the water for no-load operation in which the runner is rotationally driven by the water when the electric power generator is prevented from supplying the electric power to the electric power transmission lines, so that an operating point of the runner is moved away rapidly from the S-characteristic portion.

If, under at least one of a case in which  $\partial Q_1 / \partial N_1 > 0$ , a case in which  $\partial T_1 / \partial N_1 > 0$ , a case in which the absolute value of  $\partial Q_1 / \partial N_1$  is more than the first value, and a case in which the absolute value of  $\partial T_1 / \partial N_1$  is more than the second value, that is, in the S-characteristic portion, a transition from increase to decrease of an opening area of the flow rate adjuster occurs with a delay in phase angle not more than 120 degrees from a transition from increase to decrease of the actual rotational speed of the runner, the decrease of the actual rotational speed of the runner is suppressed by an increase in differential pressure across the turbine

caused by a change of the opening area of the flow rate adjuster and the increase of the actual rotational speed of the runner is suppressed by a decrease in differential pressure across the turbine caused by the change of the closing area of the flow rate adjuster.

If, under at least one of a case in which  $\partial Q_1/\partial N_1 > 0$ , a case in which  $\partial T_1/\partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1/\partial N_1$  is more than a first value, and a case in which an absolute value of  $\partial T_1/\partial N_1$  is more than the second value, that is, in the S-characteristic portion, a transition from decrease to increase of the opening area of the flow rate adjuster occurs with a delay in phase angle not more than 120 degrees from a transition from decrease to increase of the actual rotational speed of the runner, the decrease of the actual rotational speed of the runner is suppressed by the increase in differential pressure across the turbine caused by the change of the opening area of the flow rate adjuster and the increase of the actual rotational speed of the runner is suppressed by the decrease in differential pressure across the turbine caused by the change of the closing area of the flow rate adjuster.

If the ratio of the gain of the derivative calculation element to the gain of the integration calculation element applied to the derivative calculation element and the integration calculation element when the head of the water for driving

rotationally the runner is not more than the predetermined value is greater than the ratio of the gain of the derivative calculation element to the gain of the integration calculation element applied to the derivative calculation element and the integration calculation element when the head of the water for driving rotationally the runner is more than the predetermined value, the derivative component of the control signal effectively suppresses the undesirable oscillation in the rotational speed of the runner when the head of the water for driving rotationally the runner is not more than the predetermined value, and the acceleration in the rotational speed of the runner from zero toward the desired rotational speed thereof is kept not too slow when the head of the water for driving rotationally the runner is more than the predetermined value.

If the ratio of the gain of the derivative calculation element to the gain of the integration calculation element applied to the derivative calculation element and the integration calculation element under at least one of a case in which  $\partial Q_1 / \partial N_1 > 0$ , a case in which  $\partial T_1 / \partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1 / \partial N_1$  is more than a first value, and a case in which an absolute value of  $\partial T_1 / \partial N_1$  is more than a second value is greater than a ratio of the gain of the derivative calculation element to the gain of the integration calculation element applied to the

derivative calculation element and the integration calculation element under a case in which  $\partial Q_1/\partial N_1 \leq 0$ ,  $\partial T_1/\partial N_1 \leq 0$ , the absolute value of  $\partial Q_1/\partial N_1$  is not more than the first value, and the absolute value of  $\partial T_1/\partial N_1$  is not more than the second value, the derivative component of the control signal effectively suppresses the undesirable oscillation in the rotational speed of the runner in the S-characteristic portion, and the acceleration in the rotational speed of the runner from zero toward the desired rotational speed thereof is kept not too slow in the turbine operating range other than the S-characteristic portion.

It is preferable for controlling stably the rotational speed of the turbine in the S-characteristic portion that a variation of the control signal corresponding to the opening area of the flow rate adjuster is in advance of a variation of the input signal under at least one of a case in which  $\partial Q_1/\partial N_1 > 0$ , a case in which  $\partial T_1/\partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1/\partial N_1$  is more than a first value, and a case in which an absolute value of  $\partial T_1/\partial N_1$  is more than a second value, that is, in the S-characteristic portion. In this situation, it is preferable that the variation of the control signal is in advance of the variation of the input signal by 30-90 degrees in phase angle of variation.

It is preferable for controlling stably the rotational speed of the turbine in the S-characteristic

portion that a ratio of a gain of the derivative calculation element to a gain of the integration calculation element to be applied to the derivative calculation element and the integration calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than a predetermined degree is determined in such a manner that the variation of the control signal corresponding to the opening area of the flow rate adjuster is in advance of the variation of the input signal under at least one of a case in which  $\partial Q_1 / \partial N_1 > 0$ , a case in which  $\partial T_1 / \partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1 / \partial N_1$  is more than a first value, and a case in which an absolute value of  $\partial T_1 / \partial N_1$  is more than a second value. In this situation, it is preferable that the variation of the control signal is in advance of the variation of the input signal by 30-90 degrees in phase angle, and/or that a ratio of a gain of the derivative calculation element to a gain of the proportional calculation element to be applied to the derivative calculation element and the proportional calculation element when the difference between the actual rotational speed of the runner and the desired rotational speed of the runner is not more than the predetermined degree is determined in such a manner that the variation of the control signal is in advance of the variation of the input signal under at least one

of a case in which  $\partial Q_1/\partial N_1 > 0$ , a case in which  $\partial T_1/\partial N_1 > 0$ , a case in which an absolute value of  $\partial Q_1/\partial N_1$  is more than a first value, and a case in which an absolute value of  $\partial T_1/\partial N_1$  is more than a second value.

5                    Other objects, features and advantages of the invention will become apparent from the following description of the embodiments of the invention taken in conjunction with the accompanying drawings.

#### BRIEF DESCRIPTION OF THE SEVERAL VIEWS OF THE DRAWINGS

10                    Fig. 1A is a diagram showing a relationship between unit speed ( $N_1 = N/\sqrt{H}$ ) and unit discharge or unit discharge flow rate ( $Q_1 = Q/\sqrt{H}$ ) on each of opening degrees of wicket gate.

15                    Fig. 1B is a diagram showing a relationship between unit speed ( $N_1 = N/\sqrt{H}$ ) and unit torque ( $T_1 = T/H$ ) on each of opening degrees of wicket gate.

20                    Fig. 2 includes diagrams showing relationships among time (s), opening degree of wicket gate (Y), water (discharge) flow rate for turbine (Q), turbine output power ( $P_t$ ) and trajectory of operation point of turbine on unit discharge  $Q_1$  versus unit speed  $N_1$  plane in a dynamic simulation analysis of prior art.

25                    Fig. 3 is a block diagram showing a linearized simulation model of a turbine as a controlled object and a generator.

Fig. 4 is a block diagram showing a linearized simulation model of a turbine as a



controlled object and a generator.

Fig. 5 is a block diagram showing a linearized simulation model of a rotational speed control system including the controlled object.

5 Fig. 6 is a block diagram of a governor for a turbine in accordance with the latest International Standard version.

Fig. 7 includes diagrams showing relationships among time (s), opening degree of wicket gate (Y), water flow rate for turbine (Q), turbine  
10 output power ( $P_t$ ) and head (H) obtained by analysis on embodiment of the invention when starting in the electric power generating mode.

Fig. 8 includes diagrams showing  
15 relationships among time (s), unit discharge ( $Q_1$ ), unit speed ( $N_1$ ), rotational speed of runner (N), and outputs ( $Z_d$ ,  $Z_p$  and  $Z_i$ ) of derivative, proportional and integration calculation elements obtained by analysis on embodiment of the invention when starting in the  
20 electric power generating mode.

Fig. 9 includes diagrams showing relationships among time (s), water flow rate for turbine (Q), opening degree of wicket gate (Y), rotational speed of runner (N), head (H), and turbine  
25 output power ( $P_t$ ) obtained by analysis on embodiment of the invention when starting in the electric power generating mode.

Fig. 10 includes diagrams showing

relationships among times, and outputs ( $Z_d$ ,  $Z_p$  and  $Z_i$ ) of derivative, proportional and integration calculation elements obtained by analysis on embodiment of the invention when starting in the electric power  
5 generating mode.

Fig. 11 includes diagrams showing trajectory of operating point of turbine with reference to relationships among unit speed ( $N_1$ ) and unit discharge ( $Q_1$ ) on each of opening degrees of wicket gate ( $Y_a$  and  
10  $Y_b$ ) obtained by analysis on embodiment of the invention when starting in the electric power generating mode.

Fig. 12 is a block diagram of a governor.

Fig. 13 is a block diagram of a pump turbine apparatus with a governor of the invention.

15 Fig. 14A is a diagram showing relationships between opening degree of wicket gate ( $y$ ) and rotational speed of runner ( $N$ ) as result of operations of speed adjuster, output adjuster and speed droop circuit of governor.

20 Fig. 15 is a schematic view showing a turbine apparatus usable in the invention.

#### DETAILED DESCRIPTION OF THE INVENTION

Operational characteristics of a pump turbine as the claimed turbine is described below at first. A  
25 flow rate characteristic of the pump turbine is shown by a relationship between a unit speed ( $N_1 = N/\sqrt{H}$ ) and a unit discharge (flow rate) ( $Q_1 = Q/\sqrt{H}$ ) on each of

various opening degrees of a wicket gate as the claimed flow rate adjuster. A torque characteristic of the pump turbine is shown by a relationship between the unit speed ( $N1 = N/\sqrt{H}$ ) and a unit torque ( $T1 = T/H$ ) on each of various opening degrees of the wicket gate. These characteristics of the pump turbine are called as performance curves.

The flow rate characteristic includes a first area in which the unit discharge  $Q1$  decreases in accordance with an increase of the unit speed  $N1$  and a second area in which the unit discharge  $Q1$  decreases in accordance with a decrease of the unit speed  $N1$ . The first area includes a slack change area in which the unit discharge  $Q1$  changes relatively slack in accordance with a change of the unit speed  $N1$ , and an abrupt change area in which the unit discharge  $Q1$  changes relatively abruptly in accordance with the change of the unit speed  $N1$ . In this specification, a combination of the second area and the abrupt change area is called as S-characteristic portion. Further, the torque characteristic includes a first area in which the unit torque  $T1$  decreases in accordance with the increase of the unit speed  $N1$  and a second area in which the unit torque  $T1$  decreases in accordance with the decrease of the unit speed  $N1$ .

A regular operation of the pump turbine with a load in a generating mode is performed in the slack change area. The smaller an output power of the

turbine under a constant value of the unit speed  $N_1$  is, that is, the smaller an opening degree or area of a wicket gate is, the smaller a distance between the S-characteristic portion and the unit speed  $N_1$  at which the regular operation of the pump turbine with the load is performed with the opening degree or area of the wicket gate is. When a rotation of the pump turbine is started, particularly when an actual rotational speed of the turbine is increased to the vicinity of a rated rotational speed so that the rotation of the pump turbine is synchronized with a frequency of an electric power transmission line, the wicket gate is set at an opening degree or area suitable for no-load of the turbine, that is, a minimum opening degree for the regular operation, so that the distance between the S-characteristic portion and an area of the unit speed  $N_1$  at which area the regular operation of the pump turbine is performed becomes minimum. When an effective head  $H$  of a water is minimum, the unit speed  $N_1$  becomes maximum to decrease further the distance between the S-characteristic portion and the unit speed  $N_1$  at an operating point of the turbine. Therefore, when the actual rotational speed of the turbine is increased to the vicinity of the rated rotational speed so that the rotation of the pump turbine is synchronized with the frequency of the electric power transmission line, there is a probability of that the operating point enters into the S-characteristic portion to be

positioned at the abrupt change area of the first area.  
When a variable range of the effective head  $H$  is significantly wide and a ratio of a minimum effective head  $H$  to a datum effective head  $H$  is significantly small, the probability becomes higher at the minimum effective head  $H$ . In some cases, when the actual rotational speed of the turbine is increased to the vicinity of the rated rotational speed, there is a probability of that the operating point of the turbine enters into the second area of the S-characteristic portion. Even when the variable range of the effective head  $H$  is not significantly wide, the flow rate of the water to be supplied to the turbine so that the rotation of the turbine is started needs to be increased from zero to at least a flow rate for rotation under no-load of the turbine, whereby a water hammer occurs necessarily because of the change in flow rate of the water so that there is a probability of that the operating point temporarily enters widely into the S-characteristic portion.

Four quadrant performance curves of the pump turbine having the S-characteristics in turbine operating domain are shown in Fig. 1A in which a relationship between unit speed ( $N1 = N/\sqrt{H}$ ) and unit discharge ( $Q1 = Q/\sqrt{H}$ ) on each of opening degrees of wicket gate is shown and Fig. 1B in which a relationship between the unit speed ( $N1 = N/\sqrt{H}$ ) and unit torque ( $T1 = T/H$ ) on each of the opening degrees

of wicket gate is shown, while  $N$  is the actual rotational speed of the turbine,  $Q$  is the flow rate of the water to be supplied to the turbine,  $H$  is the effective head  $H$  of the water, and  $T$  is the torque of the turbine.

Performance curves 1 and 1' are obtained under a relatively large predetermined opening area of the wicket gate. Performance curves 2 and 2' are obtained under an opening area of the wicket gate smaller than the opening area of the wicket gate along the performance curves 1 and 1'. Performance curves 3 and 3' are obtained under an opening area of the wicket gate smaller than the opening area of the wicket gate along the performance curves 2 and 2'.

In the second area of the performance curve 1, that is, a-d-h curve area, the unit discharge  $Q_1$  decreases in accordance with the decrease of the unit speed  $N_1$ . In the second area of the performance curve 2, that is, b-e-i curve area, the unit discharge  $Q_1$  decreases in accordance with the decrease of the unit speed  $N_1$ . In the second area of the performance curve 3, that is, c-f-j curve area, the unit discharge  $Q_1$  decreases in accordance with the decrease of the unit speed  $N_1$ . As clearly shown, the a-d-h curve area in the second area of the performance curve 1 is longer than the b-e-i curve area in the second area of the performance curve 2, the b-e-i curve area in the second area of the performance curve 2 is longer than the c-f-

j curve area of the second area of the performance curve 3. Therefore, the smaller the opening area of the wicket gate is, the shorter a length of the S-characteristic portion in a direction of a coordinate axis of the unit discharge  $Q_1$  is.

Similarly to Fig. 1A, in Fig. 1B, the second area of the performance curve 1' is a'-d'-h' curve area, the second area of the performance curve 2' is, b'-e'-i' curve area, and the second area of the performance curve 3' is c'-f'-j' curve area.

Close relationships exist between Figs. 1A and 1B. For example, a point x at which  $Q_1 = Q_{1x}$  and  $N_1 = N_{1x}$  are satisfied on the performance curve 3 in Fig. 1A corresponds to a point x' on the performance curve 3' in Fig. 1B. At the point x',  $T_1 = T_{1x'}$  and  $N_1 = N_{1x'}$  ( $= N_{1x}$ ) are satisfied. Similarly, the points a, b, c, d, e, f, h, i and j in Fig. 1A correspond to the points a', b', c', d', e', f', h', i' and j' in Fig. 1B.

A curve NR is a no-load discharge curve. Cross points  $\alpha$ ,  $\beta$  and  $\gamma$  between the curve NR and the performance curves 1, 2 and 3 correspond respectively to cross points  $\alpha'$ ,  $\beta'$  and  $\gamma'$  between the performance curves 1', 2' and 3' and the  $T_1$  coordinate axis ( $T_1 = 0$ ).

For starting the operation of the turbine in the generating mode, the rotational speed needs to be increased from zero to the rated rotational speed  $N_0$

under an generator load of approximately zero, that is, the operating point is moved rightwards along the  $N_1$  coordinate axis of the  $N_1$ - $T_1$  relationship diagram from a datum point ( $N_1 = 0$ ,  $T_1 = 0$ ) obtained when being  
5 stopped to a point  $N_1 = N_0/\sqrt{H}$ . When the cross point between the  $N_1$  coordinate axis and a line of  $N_1 = N_0/\sqrt{H}$  exists between the cross points  $\alpha'$  and  $\beta'$  after the actual rotational speed  $N$  increases to the rated rotational speed  $N_0$ , the opening area of the wicket gate  
10 needs to be increased between the performance curves 1 and 2. Further, in the  $N_1$ - $Q_1$  relationship diagram, the operating point is moved from a datum point ( $N_1 = 0$ ,  $Q_1 = 0$ ) to an intermediate point between the points  $\alpha$  and  $\beta$  on the curve  $NR$ . That is, the unit discharge  $Q_1$   
15 needs to be increased from zero to the intermediate point between the points  $\alpha$  and  $\beta$  of  $Q_1$ , and the flow rate or discharge  $Q$  needs to be increased to a corresponding amount.

When the generator connected to the turbine  
20 is a synchronous generator, a rotational speed of the turbine to be required for being put on the electric power transmission line, that is, the rated rotational speed  $N_0$  is fixed, while the unit speed  $N_1$  varies in accordance with the head. When the head is of the  
25 minimum value, the actual rotational speed of the turbine needs to be synchronized with the frequency of the electric power transmission line under the maximum value of the unit speed  $N_1$ . In this case, it is



difficult for the operating point to be positioned in the slack change area of the first area of the flow rate characteristic or discharge performance curve, and there is a probability of that the operating point is  
5 positioned in the abrupt change area of the first area.

When a rotational direction of the runner is changeable to pump the water for the pumping mode as well as to be driven by the water for the electric power generating mode, the runner has a flat shape  
10 preferable for centrifugal pumping operation for pumping the water. Consequently, in the electric power generating mode, the S-characteristics, that is, a reverse flow appearing region caused by a centrifugal force tends to move to a N1 lower side, that is, the  
15 regular operating range of N1. Therefore, in the turbine for pumping the water as well as generating the electric power, when a pumping performance is improved, it tends to be difficult for the rotational speed of the turbine to be controlled stably during rotational  
20 start of the turbine in the electric power generating mode.

In this case, there is a probability of that the actual rotational speed of the turbine cannot be kept stable sufficiently for putting the electric power  
25 generator on the electric power transmission line, after the actual rotational speed of the turbine increases to the vicinity of the rated rotational speed of the turbine. Especially, when the operating point

of the turbine is positioned in the second area as the S-characteristic portion during synchronizing the actual rotational speed of the turbine with the frequency of the electric power transmission line before putting the electric power generator on the electric power transmission line, the rotational speed of the turbine cannot be adjusted in the prior art desirably for putting the electric power generator on the electric power transmission line, and an electric power generating plant including such turbine is not usable in such a value of the head.

In Fig. 2 showing analyzing or simulating results of the turbine rotational speed synchronizing control by the prior art in a case in which the operating point of the turbine is positioned in the second area as the S-characteristic portion, a diagram (A) shows a relationship between a time proceeding and each of an opening degree or area  $Y$  of the wicket gate, the flow rate  $Q$  supplied to the turbine, the actual rotational speed  $N$  of the turbine and an output power  $P_t$  of the turbine, a diagram (B) shows a relationship between a time proceeding and each of an opening degree or area  $Y$  of the wicket gate, the flow rate  $Q$  of the water applied to the turbine, and an effective head  $H$  of the water applied to the turbine, a diagram (C) shows a trajectory of the operating point of the turbine on  $N_1$ - $Q_1$  plane, and a diagram (d) shows a relationship between a time proceeding and each of an

output signal  $Z_p$  of a proportional calculation element, an output signal  $Z_i$  of an integration calculation element and an output signal  $Z_d$  of a derivative calculation element in a PID calculation device

5 receiving an input signal corresponding to a difference between the actual rotational speed of the runner and a desired rotational speed of the runner and generating an output signal corresponding to a command signal for the opening degree or area  $Y$  of the wicket gate.

10 A governor for controlling the actual rotational speed of the runner as shown in Fig. 12, includes a target speed setter G10 for setting a target rotational speed of the turbine, a comparator G11 for calculating a difference between the target rotational  
15 speed of the turbine and the actual rotational speed of the turbine, a positive-negative sign changer G01, a proportional calculation element G02, an integration calculation element G03, a derivative calculation element G04, an adder G05, a hydraulic amplifier or  
20 servo-motor G06 for driving the wicket gate and a link mechanism G07 for converting mechanically an output movement of the hydraulic amplifier or servo-motor G06 to a movement of the wicket gate for adjusting the flow rate of the water. An LVG (low value gate) G09 outputs  
25 lower one of an wicket gate opening degree limit signal generated by a wicket gate opening degree limiter G08 for limiting a maximum value  $Y_u$  of an wicket gate opening degree or area and a total amount of the output

signals  $Z_p$ ,  $Z_i$  and  $Z_d$ , so that the output signal corresponding to the wicket gate opening degree or area is prevented from having an excessive value. Before starting the rotation of the turbine, the target rotational speed is set in the vicinity of the rated rotational speed, and the maximum value  $Y_u$  of the wicket gate opening degree or area is set in such a manner that the flow rate of the water determined by the wicket gate opening degree or area is sufficient for accelerating rotationally the turbine from zero of the rotational speed and for preventing an excessive overshoot of the actual rotational speed of the turbine in comparison with the target rotational speed. As shown in the diagram of Fig. 2, when the maximum value  $Y_u$  of the wicket gate opening degree or area set by the wicket gate opening degree limiter G08 is increased from zero, the wicket gate opening degree increases gradually to increase the flow rate of the water applied to the turbine. In response to that a torque generated on the turbine by the water exceeds a static friction torque of the turbine, an increase of the actual rotational speed of the turbine starts from zero.

By setting a gain of the derivative calculation element G04 appropriately as the present invention, unstable changes of the opening degree or area  $Y$  of the wicket gate, the flow rate  $Q$  supplied to the turbine, the actual rotational speed  $N$  of the

turbine and the output power  $P_t$  of the turbine as shown in Fig. 2 are restrained. That is, by the present invention, the actual rotational speed  $N$  of the turbine is stably controlled even when the operating point of the turbine is positioned in the second area as the S-characteristic portion during an increase of the actual rotational speed of the runner from zero toward the target rotational speed of the runner, so that a range of the head in which the actual rotational speed  $N$  of the turbine is stably controlled is enlarged to a lower level the head.

A typical model of a turbine rotational speed control system to which the present invention is applicable is shown as follows. Incidentally, a water path or column extending to the turbine from each of upstream and downstream sides thereof is considered as a rigid column in accordance with the rigid column theory. Basis formulas are as follows.

$$Q = Q_0 + \Delta Q = Q_0 + \frac{\partial Q}{\partial Y} \Delta Y + \frac{\partial Q}{\partial N} \Delta N + \frac{\partial Q}{\partial H} \Delta H$$

$$\Psi = \Psi_0 + \Delta \Psi = \Psi_0 + \frac{\partial \Psi}{\partial Y} \Delta Y + \frac{\partial \Psi}{\partial N} \Delta N + \frac{\partial \Psi}{\partial H} \Delta H$$

$$\Delta H = - \frac{L}{Ag} \frac{dQ}{dt}$$

$$P_t = P_{t0} + \Delta P_t = 9.8 \Psi Q H$$

$$\frac{dN}{dt} = \frac{60^2 \times 4 \times 102g\Delta P_t}{4\pi^2 N_0 GD^2} = \frac{365000\Delta P_t}{N_0 GD^2}$$

In these formulas,  $Q$  is the flow rate ( $m^3/s$ ) of the water applied to the turbine,  $Q_0$  is an initial value of the flow rate,  $Y$  is the opening degree (pu) of the wicket gate,  $Y_0$  is an initial value of the opening degree of the wicket gate,  $N$  is the actual rotational speed (rpm) of the turbine,  $N_0$  is an initial value (rpm) of the actual rotational speed of the turbine,  $H$  is the effective head (m) of the water applied to the turbine,  $H_0$  is an initial value (m) of the effective head,  $\Psi$  is a turbine efficiency (pu),  $\Psi_0$  is an initial value of the turbine efficiency,  $L$  is a total length (m) of water columns extending to the turbine from upstream and downstream sides thereof,  $A$  is an averaged value ( $m^2$ ) of cross sectional areas of the water columns extending to the turbine from upstream and downstream sides thereof,  $g$  is the gravitational constant ( $m/s^2$ ),  $t$  is proceeding time (s),  $P_t$  is an output power (KW) of the turbine,  $P_{t_0}$  is an initial value of the output power of the turbine, and a rotational moment of inertia of a combination of the electric power generator and the turbine ( $kgf \cdot m^2$ ) :  $I$  is ( $GD^2/4g$ ) while the initial values are measurable at the proceeding time of zero.

These parameters are made dimensionless respectively by a wicket gate opening degree  $Y_r$  under

the rated output power of the turbine and the rated head, a rated turbine rotational speed  $N_r$ , the rated head  $H_r$ , the rated flow rate  $Q_r$  under the rated output power of the turbine and the rated head, the rated output power  $P_{tr}$  of the turbine, and the rated turbine efficiency  $\Psi_r$  under the rated output power and the rated head, so that  $y = \Delta Y/Y_r$ ,  $n = \Delta N/N_r$ ,  $h = \Delta H/H_r$ ,  $q = \Delta Q/Q_r$ ,  $pt = \Delta P_t/P_{tr}$  and  $\eta = \Delta \Psi/\Psi_r$  are obtained.

By setting that  $\eta_0 = \Psi_0/\Psi_r$ ,  $q_0 = Q_0/Q_r$ ,  $pt_0 = P_{t0}/P_{tr}$ ,  $h_0 = H_0/H_r$ ,  $y_0 = Y_0/Y_r$ , and  $n_0 = N_0/N_r$ , and by deeming changes of the parameters in the vicinities of the respective initial values to be negligible, the typical model of the turbine rotational speed control system to which the present invention is applicable may be expressed in linearized models as shown in Figs. 3 and 4. Incidentally,  $y$  is the opening degree of the wicket gate (p.u.) and  $pt$  is the output power of the turbine (p.u.), and  $n$  is the actual rotational speed of the turbine (p.u.).  $T_m$  is a time constant (sec) of an inertia effect of the combination of the generator and the turbine corresponding to  $(N_r N_0 G D^2)/(365000 P_{tr})$ , and  $T_w$  is a time constant (sec) of the water columns extending to the turbine from upstream and downstream sides thereof, which time constant corresponds to  $(L Q_r)/(A H_r g)$ .  $S$  is Laplace operator, and coefficients  $C_{ph}$ ,  $C_{py}$ ,  $C_{pn}$ ,  $C_{qq}$ ,  $C_{qy}$  and  $C_{qn}$  are defined as follows.

$$C_{ph} = \eta_0 q_0 + \frac{\partial Q}{\partial H} \frac{H_0}{Q_r} \eta_0 + \frac{\partial \Psi}{\partial H} \frac{H_0}{\Psi_r} q_0$$

$$C_{py} = \left( \frac{\partial Q}{\partial Y} \frac{\eta_0}{Q_r} + \frac{\partial \Psi}{\partial Y} \frac{q_0}{\Psi_r} \right) h_0 Y_r$$

$$C_{pn} = \left( \frac{\partial Q}{\partial N} \frac{\eta_0}{Q_r} + \frac{\partial \Psi}{\partial N} \frac{q_0}{\Psi_r} \right) h_0 N_r$$

$$C_{qq} = \frac{Q_r}{\frac{\partial Q}{\partial H} H_r}$$

$$C_{qy} = \frac{\frac{\partial Q}{\partial Y} Y_r}{\frac{\partial Q}{\partial H} H_r}$$

$$C_{qn} = \frac{\frac{\partial Q}{\partial N} N_r}{\frac{\partial Q}{\partial H} H_r}$$

Fig. 5 shows a typical model of a turbine rotational speed control system which includes a linearized model of a turbine as a controlled system as shown in Figs. 3 and 4 and a linearized PID type governor or control device as enclosed by dot-line in Fig. 5, and to which the present invention is



applicable. The turbine rotational speed control system includes the positive-negative sign changer G01, the proportional calculation element G02, the integration calculation element G03, the derivative calculation element G04, the adder G05, the hydraulic amplifier or servo-motor G06 for driving the wicket gate and the link mechanism G07 for converting mechanically the output movement of the hydraulic amplifier or servo-motor G06 to the movement of the wicket gate for adjusting the flow rate of the water.  $K_p$  is a gain of the proportional calculation element G02,  $K_i$  is a gain of the integration calculation element G03,  $K_d$  is a gain of the derivative calculation element G04,  $T_y$  is a time constant of the hydraulic amplifier or servo-motor G06, and  $K_{gy} = y/y_{sv}$ .

A basic concept of the invention is explained below. A rotational speed control of the turbine according to the invention is not performed by using a stationary control factor  $C_{py}$ , but is performed by using a transient control factor or a water hammer factor which is generated along  $C_{qy}$  having positive value in the S-characteristic portion in which  $\partial_1/\partial N_1 > 0$  and/or  $\partial T_1/\partial N_1 > 0$  and  $C_{qh}$  having negative value in the S-characteristic portion in which  $\partial Q_1/\partial_1 > 0$  and/or  $\partial T_1/\partial N_1 > 0$  in a control loop  $y \rightarrow h \rightarrow p_t \rightarrow n \rightarrow \text{governor} \rightarrow y$ . By making the gain  $K_d$  of the derivative calculation element significantly greater than the gains of the other calculation elements, the transient power effect by the

water hammer factor  $-C_{qy}$ .  $C_{qh}$  can be made significant in the S-characteristic portion in which  $\partial Q_1/\partial N_1 > 0$  and/or  $\partial T_1/\partial N_1 > 0$  as compared with the stationary power effect by the stationary power factor  $C_{py}$  based on the stationary

5 wicket gate opening versus turbine output power relation. Besides, by making the gain  $K_d$  of the derivative calculation element significantly greater than the gains of the other calculation elements, the transient power factor by the water hammer  $-C_{qy}$ .  $C_{qh}$

10 can be made to work timely for the speed control, since the phase shift of the speed control signal through the governor becomes nearly 90 degree in advance phase and accordingly the resultant power can be made to change nearly in phase with the input signal to the governor

15 PID circuits. For example, when the rotational speed  $n$  decreases in the second area as the S-characteristic portion, the opening degree  $y$  of the wicket gate is increased to decrease the flow rate of the water in the S-characteristic portion so that the water hammer is

20 generated timely to increase a pressure difference across the turbine. By increasing the pressure difference across the turbine, the turbine output is increased timely and the decrease of the rotational speed  $n$  of the turbine is prevented or restrained so

25 that the rotational speed  $n$  is controlled stably.

When the head  $H$  is in the vicinity of the rated head or the rotational speed of the turbine is relatively low during increase of the actual rotational

speed of the turbine from zero toward the desired rotational speed,  $N_1 (= N/\sqrt{H})$  does not become significantly high and the operating point of the turbine is not positioned in the second area as the S-characteristic portion. In other words, when the head  $H$  is in the vicinity of its minimum value or the rotational speed of the turbine is in the vicinity of the rated rotational speed, there is a probability of that the operating point of the turbine is positioned in the second area as the S-characteristic portion. Therefore, the gain  $K_d$  of the derivative calculation element should be made significantly greater than the gains of the other calculation elements when the head  $H$  is in the vicinity of its minimum value or the rotational speed of the turbine is in the vicinity of the rated rotational speed. If the gain  $K_d$  of the derivative calculation element is made significantly greater than the gains of the other calculation elements also in case of that the head  $H$  is not in the vicinity of its minimum value or the rotational speed of the turbine is not in the vicinity of the rated rotational speed, that is, in case of that the operating point of the turbine is positioned in the first area of the S-characteristic or an area other than the S-characteristic portion, there is a probability that the rotational speed control by the governor becomes too sluggish because the gain  $K_i$  of the integration calculation element and the gain  $K_p$  of

the proportional calculation element can not be set sufficiently high even if there is no such need. Therefore, it is preferable that the gain  $K_d$  of the derivative calculation element is made significantly greater than the gains of the other calculation elements when the head  $H$  is in the vicinity of its minimum value or the rotational speed of the turbine is in the vicinity of the rated rotational speed, and the the gain  $K_d$  of the derivative calculation element is prevented from being made significantly greater than the gains of the other calculation elements when the head  $H$  is not in the vicinity of its minimum value or the rotational speed of the turbine is not in the vicinity of the rated rotational speed.

15           A PID type speed governor for the turbine in accordance with the latest IEC International Standard 61362 (Guide to Specification of Hydraulic Turbine Control Systems) First Edition is formed as shown in Fig. 6, and includes an adder  $G_{11}$ , a proportional  
20 calculation element  $G_{12}$ , an integration calculation element  $G_{13}$ , a derivative calculation element  $G_{14}$ , an adder  $G_{15}$ , and a speed droop circuit  $G_{16}$  as a feed back circuit for obtaining  $y$  proportional to  $x$ . A value of  $x$  in the IEC International Standard corresponds to  $n$  in  
25 Fig. 5. A speed droop  $b_p$  is neglected in Fig. 5, because it does not have significant effect on the transient phenomenon of the governor. The gain  $K_p$  of the governor in Fig. 6 is the same as the gain  $K_p$  of

the governor in Fig. 5, the gain  $K_i$  of the governor in Fig. 5 corresponds to  $K_i (= K_p/T_i)$  of the governor in Fig. 6, and the gain  $K_d$  of the governor in Fig. 5 corresponds to  $K_d (= K_p T_v)$  of the governor in Fig. 6.

5  $T_{1d}$  in Fig. 6 is neglected in Fig. 5, because of a significantly small value thereof. A time constant  $T_y$  of a hydraulic amplifier in Fig. 5 is neglected in Fig. 6. During increase of the actual rotational speed of the turbine from zero toward the rated rotational speed

10 of the turbine, in response to that the actual rotational speed increases to the vicinity of the rated rotational speed, the gain  $K_i$  of the integration calculation element is significantly decreased and the gain  $K_d (= K_p T_v)$  of the derivative calculation element

15 is increased or kept constant so that a derivative calculation emphasizing setting of the governor is brought about. Further, the gain  $K_p$  of the proportional calculation element may be decreased with the decrease of the gain  $K_i$  of the integration

20 calculation element to more effectively bring about the derivative calculation emphasizing setting.

After the actual rotational speed of the runner is synchronized with required frequency of alternating electric current of electric power

25 transmission lines, and subsequently the electric power generator is electrically connected to the electric power transmission lines to supply the electric power from the electric power generator to the electric power

transmission lines, it is preferable that the opening degree of the wicket gate is rapidly increased to a degree more than a predetermined degree to move the operating point of the turbine away from the S-characteristic portion in such a manner that a sudden output power drop of the generator causing a withdrawal of electric power from the power transmission line into the generator is prevented from occurring in the S-characteristic portion. If more than 2-3 seconds elapses without the rapid increase of the opening degree of the wicket gate after the actual rotational speed of the runner is synchronized with required frequency of alternating electric current of electric power transmission lines, and subsequently the electric power generator is electrically connected to the electric power transmission lines, there is a probability of that a torque for keeping the rotational speed of the turbine and the generator constant decreases rapidly and the output power of the generator becomes less than zero to withdraw the electric power from the power transmission line into the generator, that is, to pump the water although the generator must generate the electric power. Therefore, both a rapid start of increasing the opening degree of the wicket gate and an increase of the opening degree of the wicket gate more as fast as possible are necessary so that the operating point is moved rapidly away from the S-characteristic portion.

In the latest IEC International Standard for the governor, an adjustable range of the gain  $K_p$  of the proportional calculation element is 0.6-10. According to the present invention for the speed control of the turbine in the S-characteristics, the gain  $K_p$  of the proportional calculation element is significantly decreased from the adjustable range of the latest IEC International Standard to bring about the derivative calculation emphasizing setting. Although an adjustable range of the gain  $T_v$  of the derivative calculation element is 0-2 in the latest IEC International Standard and subsequently an adjustable range of the derivative gain  $K_d (=K_p T_v)$  is 0-1.2 even when the gain  $K_p$  of the proportional calculation element is set at 0.6 of the minimum value, the derivative gain  $K_d (=K_p T_v)$  for the derivative calculation emphasizing setting needs to be not less than 5 in the present invention.

During performing the derivative calculation emphasizing setting, a control signal corresponding to the opening degree or area of the wicket gate is mainly changed by the derivative calculation element while the integration calculation element maintains its output almost constant and without participating in the speed control when a periodic variation of the speed signal to the governor is relatively short cycle not more than 50 seconds. And, only when the variation of the input signal has a relatively long cycle, the integration

calculation element participates in the speed control. Since the derivative calculation element generates a derivative component of the control signal having a progress of 90 degrees in phase from a variation wave of an input signal  $-N$ , and the integration calculation element generates an integral component of the control signal having a delay of 90 degrees in phase from the variation wave of the input signal  $-N$ , a ratio of the gain of the integration calculation element to the gain of the derivative calculation element needs to be significantly small to prevent a value of the control signal from being affected significantly by an integral component of the control signal generated by the integration calculation element during the performing the derivative calculation emphasizing setting.

Therefore, a variation wave of the control signal has a progress of 90 degrees in phase from the variation wave of the input signal  $-N$  and a delay of 90 degrees in phase from the variation wave of the input signal  $N$ .

Since the hydraulic amplifier or servo-motor for moving the wicket gate has a delay of its output movement, a variation wave of the movement or opening degree of the wicket gate has a delay slightly greater than 90 degrees from the input signal  $N$ .

Since the wicket gate opening to water hammer to turbine output routine through the coefficients  $C_{qy}$  and  $C_{ph}$  accompanies about 90 degree phase delay in total including sign reversal or 180 degree phase shift



at the flow rate to water hammer conversion portion as obvious from Fig. 5, it is preferable that the phase advancing shift through the governor including the hydraulic amplifier is adjusted to be not less than 30  
5 degree so that the overall phase delay from the governor input signal to the turbine output change can be made 60 degree or smaller.

A turbine apparatus as shown in Fig. 13, includes a speed sensor 1 for generating a turbine  
10 speed signal  $X_n$  corresponding to the actual rotational speed  $N$  of the turbine as the claimed turbine, a speed setter 2 for generating a target speed signal  $X_o$  corresponding to the desired or target rotational speed of the turbine, and an adder 3 for generating a  
15 deviation signal  $X_e$  corresponding to a total amount of a difference between the turbine speed signal  $X_n$  and the target speed signal  $X_o$  (corresponding to the difference between the actual rotational speed  $N$  and the desired or target rotational speed) and a feed back signal  $X_o$   
20 generated by a speed droop circuit, so that the deviation signal  $X_e$  is input to PDI calculation device.

When the actual rotational speed  $N$  increases from zero to a predetermined value, a proportional calculation element 4a of relatively high gain  $K_{pa}$  is  
25 used in the PDI calculation device. When the actual rotational speed  $N$  exceeds the predetermined value, a proportional calculation element 4b of relatively low gain  $K_{pb}$  ( $\ll K_{pa}$ ) is used in the PDI calculation device.

Switching between the proportional calculation elements 4a and 4b is performed by pairs of contacts 19a and 19b. For example,  $K_{pa}$  is 2.3 and  $K_{pb}$  is 0.1. When the actual rotational speed  $N$  increases from zero to the predetermined value, an integration calculation element 5a of relatively high gain  $K_{ia}$  is used in the PDI calculation device. When the actual rotational speed  $N$  exceeds the predetermined value, the integration calculation element 5b of relatively low gain  $K_{ib}$  ( $\ll K_{ia}$ ) is used in the PDI calculation device.

Switching between the integration calculation elements 5a and 5b is performed by the pairs of contacts 19a and 19b. For example,  $K_{ia}$  is 0.2 and  $K_{ib}$  is 0.02. Each pair of contacts 19a and 19b is applied to respective one of a pair of the proportional calculation elements 4a and 4b and a pair of the integration calculation elements 5a and 5b so that both the switching between the proportional calculation elements 4a and 4b and the switching between the integration calculation elements 5a and 5b are simultaneously brought about.

A derivative calculation element 6 has a fixed significantly high gain  $K_d$ , for example, 12 so that the derivative calculation emphasizing setting is performed when the actual rotational speed  $N$  exceeds the predetermined value.

A signal  $Z_p$  from the proportional calculation element 4a or 4b, a signal  $Z_i$  from the integration calculation element 5a or 5b and a signal  $Z_d$  from the

derivative calculation element 6 are added to each other by an adder 7 to generate a signal  $\Sigma Z$ . A low value gate 23 generates a control signal  $Z$  corresponding to smaller one of the signal  $\Sigma Z$  and a wicket gate maximum opening degree limiting signal  $Y_u$  set by a wicket gate maximum opening degree or load limiter 22, so that an output signal from the low value gate 23 is prevented from exceeding the wicket gate maximum opening degree limiting signal  $Y_u$ .

10 Incidentally, when the wicket gate maximum opening degree limiting signal  $Y_u$  is smaller than the signal  $\Sigma Z$ , the signal  $Z_i$  from the integration calculation element 5a or 5b being used is prevented from having an excessive value. Incidentally, the control signal  $Z$

15 corresponds to an ordered or target opening degree or area of the wicket gate. A signal  $Y$  corresponds to an actual value of the opening degree or area of the wicket gate.

A hydraulic amplifier device includes an

20 adder 8, a limiter 9 and a hydraulic servo mechanism or motor 10 for moving the wicket gate, so that a first order lag function with wicket gate traveling speed limiter is formed, and the wicket gate is moved in such a manner that a difference (corresponding to a signal

25  $Y_{\&1}$ ) between the ordered or target opening degree or area of the wicket gate corresponding to the control signal  $Z$  and the actual value of the opening degree or area of the wicket gate corresponding to the signal  $Y$

is decreased or minimized. The limiter 9 receiving the signal  $Y_{\epsilon 1}$  limits opening speed of the wicket gates to  $\theta_R/T_y$  and closing speed of the wicket gates to  $\theta_L/T_y$ . The signal  $Y_{\epsilon 1}$  corresponds to a displacement of a distributing valve without a displacement limiter and the signal  $Y_{\epsilon 2}$  corresponds to a displacement of the distributing valve with the displacement limiter.

In an adder 11, the signal  $Y$  corresponding to the actual value of the opening degree or area of the wicket gate and a wicket gate opening degree setting signal  $Y_a$  generated by an output adjuster 13 and corresponding to a desired output power are added to each other. During the increase of the actual rotational speed of the turbine from zero toward the target actual rotational speed of the turbine, the wicket gate opening degree setting signal  $Y_a$  has a value corresponding to an opening degree of the wicket gate suitable for no-load rotation of the turbine. When the opening degree of the wicket gate set for no-load operation of the turbine is greater than the actual value of the opening degree or area of the wicket gate, an opening signal of  $\sigma (Y_a - Y)$  is continuously input into the PID calculation device so that a difference between the opening degree of the wicket gate set for no-load rotation of the turbine and the actual value of the opening degree or area of the wicket gate becomes zero. The coefficient  $\sigma$  is set by a speed droop circuit 12. in other words, the

coefficient  $\sigma$  is a gain between the turbine speed  
signal  $X_n$  corresponding to the actual rotational speed  
 $N$  of the turbine and the signal  $Y$  corresponding to the  
actual value of the opening degree or area of the  
5 wicket gate, and usually have a fixed value determined  
on the basis of role of the electric generation plant,  
that is, a load bearing ratio of the electric  
generation plant in the electric power transmission  
system. A block 14 shows a combination of the turbine  
10 which is driven by the water adjusted by the wicket  
gate and the electric generator driven by the turbine.

Operations of the speed setter 2, output  
adjuster 13 and speed droop circuit 12 are explained  
with reference to Fig. 14A which corresponds to the  
15 operations just before the generator is electrically  
connected to the power transmission line to supply the  
electric power from the generator to the power  
transmission line and Fig. 14B which corresponds to the  
operations after the generator is electrically  
20 connected to the power transmission line to supply the  
electric power from the generator to the power  
transmission line. In Fig. 14A, a solid line  
descending from left to right indicates a relationship  
between the signal  $Y$  corresponding to the actual value  
25 of the opening degree or area of the wicket gate and  
the actual rotational speed of the turbine to be  
applied to the derivative calculation element and the  
integration calculation element when the turbine

rotates at the desired or target rotational speed ( $N$  (pu) is 1.00) with the wicket gate opening degree 0.2 (pu) and no turbine load. When the rotation of the turbine is started, a line indicating the relationship between the signal  $Y$  corresponding to the actual value of the opening degree or area of the wicket gate and the actual rotational speed of the turbine is positioned below the solid line by the speed setter 2, as shown in a dot line. If the wicket gate opening degree is fixed to 0.2 (pu) as shown in Fig. 14A when the turbine is rotated with no turbine load, the rotational speed of the turbine is changed by the speed setter 2. In Fig. 14B, a solid line descending from left to right indicates a relationship between the signal  $Y$  corresponding to the actual value of the opening degree or area of the wicket gate and the actual rotational speed of the turbine to be applied to the derivative calculation element and the integration calculation element when the turbine rotates at the desired or target rotational speed ( $N$  (pu) is 1.00) with the actual value of the opening degree or area of the wicket gate of 1.0 (pu) corresponding to the signal  $Y$ , that is, 100% or full turbine load or output. Just after the generator is electrically connected to the power transmission line to supply the electric power from the generator to the power transmission line, that is, when the turbine rotates with extremely small load or output power, as shown in Fig. 14B, a line

indicating the relationship between the signal Y corresponding to the actual value of the opening degree or area of the wicket gate and the actual rotational speed of the turbine is positioned below the solid line, as shown in a dot line. After the generator is electrically connected to the power transmission line to supply the electric power from the generator to the power transmission line, the turbine with the load or output power should rotate correctly at the desired or target rotational speed ( $N$  (pu) is 1.00), whereby the line indicating the relationship between the signal Y corresponding to the actual value of the opening degree or area of the wicket gate and the actual rotational speed of the turbine is moved along a line of  $N = 1.00$  horizontally by the output adjuster 13 between the solid line and the dot line in Fig. 14B. When the frequency of the electric power transmission line increases from  $N=1.00$  to  $N=1.03$  while the turbine operates along the solid line for  $N=1.00$  and  $Y=1.0$  in Fig. 14B, the actual value of the opening degree or area of the wicket gate decreases  $Y=1.0$  to  $Y=0.2$ . When the frequency of the electric power transmission line increases from  $N=1.00$  to  $N=1.015$  while the turbine operates along the solid line for  $N=1.00$  and  $Y=1.0$  in Fig. 14B, the actual value of the opening degree or area of the wicket gate decreases  $Y=1.0$  to  $Y=0.6$ . A proportional rate between a change of the frequency of the electric power transmission or a required or target

rotational speed of the turbine and a change of the actual value of the opening degree or area of the wicket gate is adjusted by the speed droop circuit 12. By increasing the gain of the speed droop circuit 12, an inclination degree of the solid line descending from left to right is increased, and a gain of a change of the actual value of the opening degree or area of the wicket gate with respect to the change of the frequency of the electric power transmission or the required or target rotational speed of the turbine is decreased.

Incidentally, the operating point of the turbine 14 in Fig. 13 having  $N_1=0$  and  $Q_1=0$  obtained before the turbine rotation start moves into the S-characteristic portion of reverse flow appearing region in which  $\partial Q_1 / \partial N_1 > 0$ , under an extremely low head of the water for driving the turbine. In this case, the water starting time  $T_w$  of the water columns for the turbine is 2.87 (s) and the mechanical starting time  $T_m$  of a rotary inertia of the generator and the turbine is 16.2 (s).

The operation of the turbine apparatus as shown in Fig. 13 from the turbine rotation start to the synchronization of the actual turbine rotation with the desired rotation turbine rotation is simulated by a computer as shown in Figs. 7-12. A difference in condition between the turbine rotational speed synchronizing control of the turbine apparatus as shown in Fig. 13 and the turbine rotational speed



synchronizing control from which the simulating results as shown in Fig. 2 is obtained is that the derivative calculation emphasizing setting as described above is brought about in the turbine apparatus as shown in Fig. 13, but is not brought about in the turbine rotational speed synchronizing control from which the simulating results as shown in Fig. 2 is obtained.

As shown in an upper diagram of Fig. 7, the actual value of the opening degree or area of the wicket gate and the flow rate of the water applied to the turbine start to increase at an elapsed time of 10 seconds, but the actual rotational speed of the turbine is kept at zero until the torque generated by the turbine becomes more than the static frictional torque of the turbine at the elapsed time of 48 seconds. At the elapsed time of 58 seconds, a feed back control of the actual value of the opening degree or area of the wicket gate on the basis of the actual rotational speed of the turbine by the governor is started with  $K_p=2.3$ ,  $K_i=0.2$  and  $K_d=12$ . At the elapsed time of about 60 seconds, in response to that the actual rotational speed of the turbine reaches the predetermined value,  $K_p$  is changed from 2.3 to 0.1 and  $K_i$  is changed from 0.2 to 0.02 so that the derivative calculation emphasizing setting is performed. Incidentally, the opening degree or area of the wicket gate is prevented from exceeding the starting opening degree thereof by the wicket gate opening degree limiter. At the elapsed

time of 120 seconds, the desired or target rotational speed of the turbine is gradually decreased so that the actual rotational speed of the turbine is synchronized with the frequency of the electric power transmission line. As clearly understood from a comparison with the top diagram of Fig. 2 and the upper diagram of Fig. 7, the actual rotational speed of the turbine is completely stable sufficiently for synchronizing the rotation of the turbine with the frequency of the electric power transmission line. As shown in lower diagram of Fig. 7, the actual flow rate of the water is decreased when the opening degree or area of the wicket gate is increased, and the actual flow rate of the water is increased when the opening degree or area of the wicket gate is decreased, that is, the operating point of the turbine is positioned in the reverse flow appearing region of the S-characteristic portion. Further, a variation curve of the opening degree or area of the wicket gate and a variation curve of the effective head or differential pressure across the turbine are reversed with respect to each other. An upper diagram of Fig. 8 shows a variation of the operating point of the turbine from the turbine rotation start to the synchronization of the actual turbine rotation with the desired turbine rotation on the  $N_1$ - $Q_1$  plane. The operating point of the turbine is converged to a extremely small region in contrast to the third diagram of Fig. 2. As shown in a lower

diagram of Fig. 8, after the derivative calculation emphasizing setting, the output  $Z_p$  of the proportional calculation element becomes substantially zero, and a change of the output  $Z_i$  of the integration calculation element becomes gradual. Therefore, the difference between the actual rotational speed of the turbine and the target rotational speed of the turbine is minimized mainly by the output  $Z_d$  of the derivative calculation element. Incidentally, a transition from increase to decrease of the output  $Z_d$  occurs with a delay in phase angle of about 90 degrees from a transition from increase to decrease of the actual rotational speed of the turbine, and a transition from decrease to increase of the output  $Z_d$  occurs with a delay in phase angle of about 90 degrees from a transition from decrease to increase of the actual rotational speed of the turbine. As shown in Fig. 9, in response to decrease of the actual rotational speed of the turbine, the opening degree or area of the wicket gate is increased to decrease the flow rate of the water so that the differential pressure across the turbine is increased to restrain or prevent the decrease of the actual rotational speed of the turbine. As shown in Fig. 10, after the derivative calculation emphasizing setting, the changes of the output  $Z_p$  of the proportional calculation element and the output  $Z_i$  of the integration calculation element are gradual so that the outputs  $Z_p$  and  $Z_i$  are not effective for minimizing the

difference between the actual rotational speed of the turbine and the target rotational speed of the turbine, and the difference between the actual rotational speed of the turbine and the target rotational speed of the turbine is minimized mainly by the output  $Z_d$  of the derivative calculation element. As shown in an upper diagram of Fig. 11, the actual rotational speed of the turbine is gradually decreased to be synchronized with the frequency of the electric power transmission line, and the operating point moves along the flow rate line on no turbine load from right to left. As understood from this diagram, the actual opening degree or area of the wicket gate obtained when the synchronization of the actual rotational speed of the turbine with the frequency of the electric power transmission line is finished is closer to  $Y_a$  than  $Y_b$ . Further, from the  $N_1$ - $Q_1$  curves of  $Y_a$  and  $Y_b$  of the opening degree of the wicket gate, it is recognizable that the operating point of the turbine moves in the reverse flow appearing region of the S-characteristic portion. As shown in a lower diagram of Fig. 11, the operating point moves substantially along a line of  $T_1 = 0$  from right to left to be controlled for synchronizing. From the the  $N_1$ - $T_1$  curves of  $Y_a$  and  $Y_b$  of the opening degree of the wicket gate on the  $N_1$ - $T_1$  plane, it is recognizable that the operating point of the turbine moves in the reverse flow appearing region of the S-characteristic portion.

It should be further understood by those skilled in the art that although the foregoing description has been made on embodiments of the invention, the invention is not limited thereto and  
5 various changes and modifications may be made without departing from the spirit of the invention and the scope of the appended claims.